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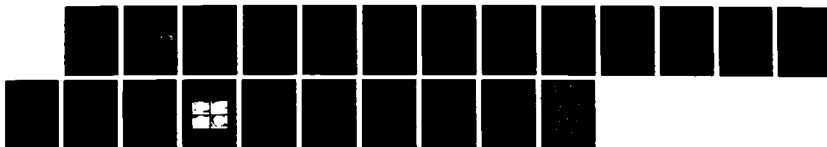
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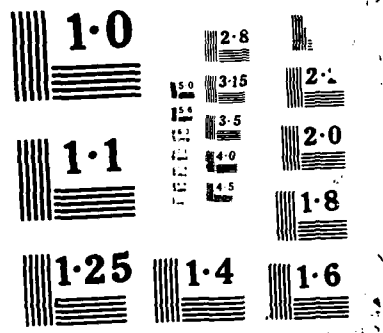
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Bimodular Behavior and Crack Closure in Compression in a Brittle Material

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30 September 1986

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achieved to enable unimpeded stress transfer across the fracture surface during vibration.

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BIMODULAR BEHAVIOR AND CRACK CLOSURE
IN COMPRESSION IN A BRITTLE MATERIAL

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1. INTRODUCTION

The presence of cracks in brittle materials can have a significant effect on the measured elastic properties. Numerous studies have investigated this effect experimentally in rock (Ref. 1), graphite (Ref. 2), and ceramics (Ref. 3); the effect has also been studied from a purely theoretical viewpoint (Ref. 4). Resonance techniques have been used to measure elastic properties in materials containing microcracks (Refs. 3 and 5). Such macroscopically measured properties have sometimes been used to replace certain microscopic quantities (Ref. 3) that are difficult to determine experimentally, such as mean microcrack radius, $\langle a \rangle$, and number density of microcracks, N .

In this experiment, the effect on the apparent elastic modulus of a single large crack, consisting of a complete fracture through the sample, was determined under compressive loading across the fracture surface. Sonic resonance was used because it can detect the change in modulus due to a single known and observable crack.

2. EXPERIMENTAL

The experiment measured the sonic resonance of a simply supported, axially loaded thin beam of graphite. The material was a 3.2-mm- (0.125-in.)-diameter, high purity carbon spectrograph rod [bulk density, $1.58 \times 10^{-3} \text{ kg/m}^3$ (1.58 g/cm^3); apparent density (flotation method), $1.93 \times 10^{-3} \text{ kg/m}^3$ (1.93 g/cm^3); porosity, 18 vol%]. The sonic resonance method is similar in principle to methods described elsewhere (Refs. 6 and 7). The beam was supported by sharply pointed metal contacts in the centers of the end faces.

Resonance was excited by placing the sample in the field of a cobalt-samarium permanent magnet and passing an ac current through the sample. The Lorentz force on the sample produces an oscillating force perpendicular to the magnetic field and the direction of current flow. The sample was observed with a binocular microscope. The frequency was varied until the resonance peak was observed; the peak is easily visible as a smearing into a line of a point viewed on the sample. The resonance frequency could be located repeatedly to a precision of better than 1% each time. Stroboscopic illumination was occasionally used to freeze the sample motion to verify that the resonance was the fundamental transverse vibrational mode.

The sample was mounted vertically between the current-carrying point contacts at the ends (Fig. 1), and the top contact was mounted on a flexible support to which weights could be added so that the sample could be axially loaded during vibration. Resonance frequency, which was measured as a function of end loading, decreased with increasing load. The load was restricted to less than approximately one-half the Euler critical buckling load, P_b , to avoid breaking the sample.

The frequency versus load was measured on the same sample, both as-machined and then after fracture at the midpoint. The 3.2-mm- (0.125-in.)-diameter graphite rod, which was 40 mm long, was machined with a single edge notch at the midpoint, 0.2 mm wide and 0.2 mm deep, aligned perpendicular to the sample axis, to facilitate subsequent fracture at that location. A small piece of adhesive tape, about $1 \times 4 \text{ mm}$, was placed on the sample to aid in

maintaining orientation of the two faces after fracture. The tape had a negligible effect on the measured frequency, because its mass was small and its modulus low compared with those of the graphite rod.

After a number of measurements of frequency versus load were taken on the sample, the rod was carefully and completely fractured through at the notch. The fractured ends were then mated together, the sample was replaced in the holder, and another series of frequency versus load measurements was made. The fracture faces were photographed stereographically in the scanning electron microscope (SEM) to observe the degree of matching of the fracture faces (see Fig. 4, p. 9).

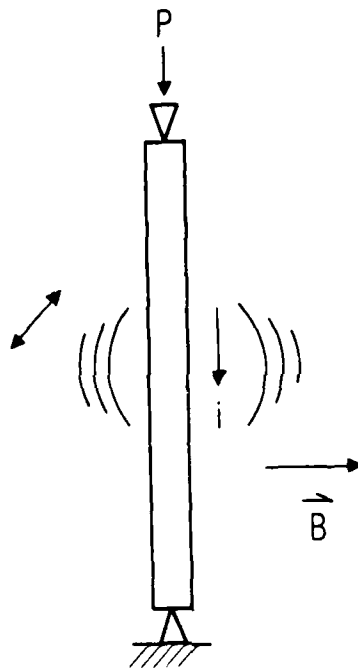


Fig. 1. Schematic of Sonic Resonance Experiment

3. THEORY

3.1 SIMPLY SUPPORTED BEAM WITH AXIAL LOADING

According to the theory of simple vibrating beams (Ref. 8), a beam supported at each end such that at the ends the displacements and the bending moments are zero (both $y = 0$ and $y'' = 0$ at $x = 0$ and $x = L$) has a frequency in the lowest mode of

$$f_0 = \frac{1}{2L} P_b^{1/2} (\rho A)^{-1/2} \quad (1)$$

where L is beam length, P_b is the Euler buckling load, ρ is the bulk mass density, and A is the cross-sectional area. The term P_b is expressed as

$$P_b = \frac{\pi^2 EI}{L^2} \quad (2)$$

where E is the Young's modulus and I is the moment of inertia of the cross section.

If an axial compressive load, P , is imposed on the beam at the supports, the frequency of the lowest transverse vibrational mode becomes (Ref. 8)

$$f = f_0 (1 - P/P_b)^{1/2} \quad (3)$$

where f_0 (frequency of the unloaded beam) is given in Eq. (1). In the graph of the behavior of f versus P , Fig. 2, as P approaches P_b the frequency approaches zero, which is to be expected since the beam is unstable with respect to a small transverse deflection at the buckling load, since the restoring force approaches zero. This relation between axial load, frequency, and modulus can be used in analyzing the experiment being discussed.

3.2 AXIALLY LOADED BEAM WITH CRACKS

Next we consider the effect of cracks on the vibrational behavior of an axially loaded beam. Assuming a number of thin planar cracks in the material, all oriented perpendicular to the beam axis, we expect the stiffness of the beam in bending to be less than that for an uncracked beam. The rationale is

that, whereas cracks might close on the compression side of the neutral axis, they would remain open on the tension side and hence no stress transfer would occur across the crack faces. Crack closure would make the material bimodular, with a higher Young's modulus in compression than in tension. If cracks did not become closed on the compression side, because the strains generated during bending were small compared with the crack-opening displacement, no bimodular effect on the apparent stiffness would be evidenced.

Changes in vibrational frequency are expected for an axially loaded beam, because the effective modulus would be higher than in the relaxed state, if the stress in the material created by the axial load were sufficient to close the cracks. During small vibrations, the cracks could remain closed, provided that the maximum tensile stress created by bending remained smaller than the compressive stress caused by the axial load. The beam would effectively be prestressed and would everywhere remain under residual compression in the axial direction.

If such crack closure were to occur at some level of axial loading, then Eq. (3) would no longer hold as originally stated, because P_b , and hence f_0 , would depend on P , since E would change with P . A simple system that illustrates this behavior, consisting of a beam with many small annular cracks in the surface, is discussed in the Appendix.

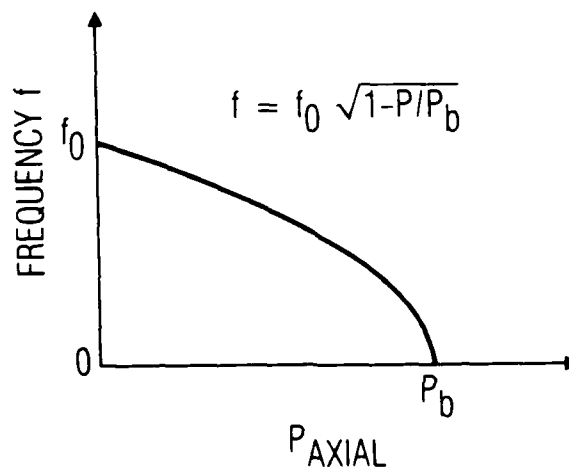


Fig. 2. Frequency versus Axial Load

4. DISCUSSION

The experiment described above can be discussed in terms of the concepts of crack closure with increased stress transfer during loading. Figure 3 plots the results of the frequency versus load experiment for the same specimen, uncracked and cracked. While f decreased with increasing load in the uncracked case up to a load of about one-fourth the extrapolated buckling load, the sample after fracture behaved the opposite: Near zero load, f_0 (cracked) was about 50% of f_0 (uncracked); as load was applied to the cracked sample, frequency initially increased; and at P of about 25% of P_b of the uncracked specimen, the frequencies for both the cracked and uncracked samples were approximately the same, indicating that stress transfer across the crack faces was similar to that in unbroken material. The transfer occurs at an equivalent stress of about 0.83 MPa (120 psi), based on the cross-sectional area of the rod.

SEM stereographic pairs of the fracture surfaces of the graphite rod (Fig. 4) depict both surfaces as having a high degree of surface roughness and as matching well (hills and valleys occur in corresponding locations). Yet when the surfaces are initially placed in contact, under small load, the load is not transferred uniformly across the interface, as indicated by the frequency, which is lower than that of the unbroken sample. Only after the load has reached a certain level does the frequency of the cracked sample become indistinguishable from that of the uncracked one. Although well matched initially, the fracture faces sustain enough damage or distortion to prevent them from seating together sufficiently for uniform stress transfer below a particular load. Once that load across the crack faces is achieved, the sample behaves elastically, as if the crack were not present, because the fracture faces remain in net compressive loading throughout the full vibrational cycle. This also shows that surface roughness of a crack is, in addition to the elastic behavior of the unbroken material surrounding the crack, an important factor in crack reclosure.

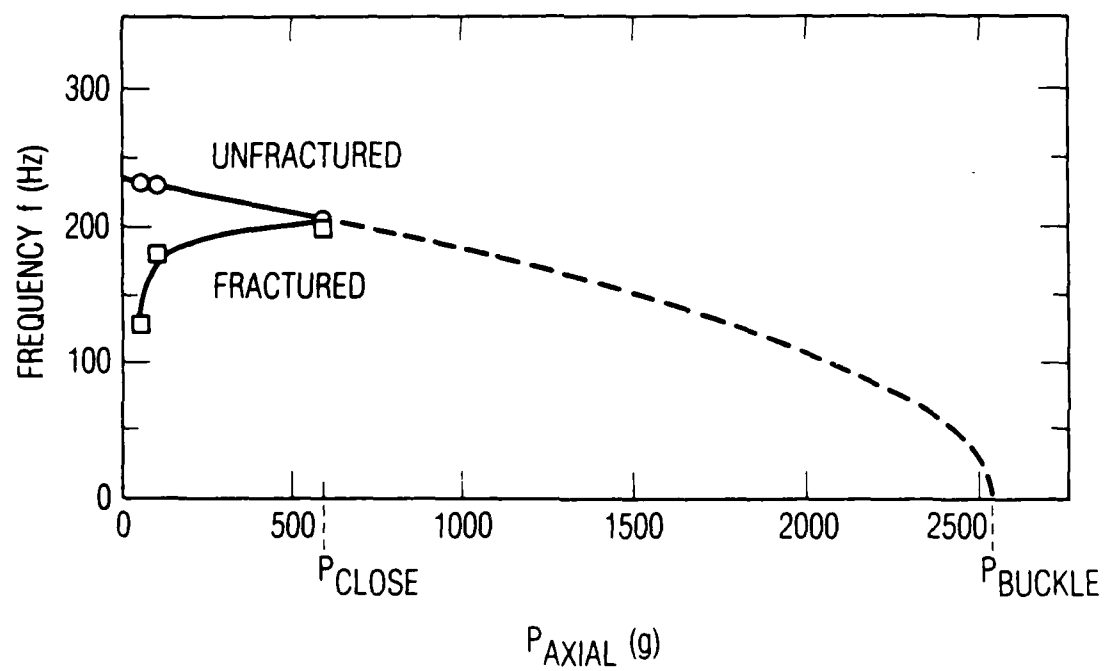


Fig. 3. Frequency versus Axial Load for Sample before and after Fracture

As a final observation, graphite is an ideal material for this experiment, because it combines high electrical conductivity and brittle fracture. Nonconductive brittle materials can also be made to resonate by applying a thin conductive stripe, such as metal film or conductive paint, along the specimen.

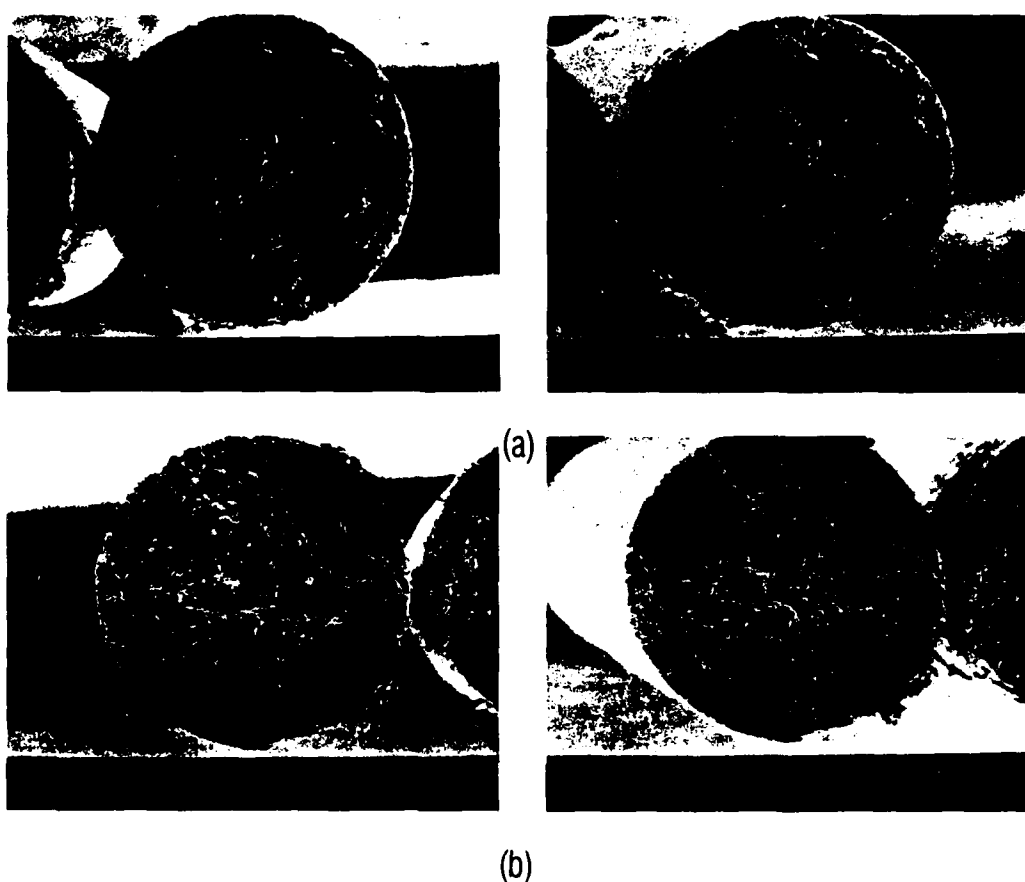


Fig. 4. Stereomicrographs of Fracture Surfaces: (a) top surface, and (b) bottom surface.

5. CONCLUSION

This experiment demonstrated that the presence of a simple fracture surface perpendicular to the beam axis in a graphite beam lowers its apparent modulus in sonic resonance. At a critical compressive stress, however, the fracture faces are brought back into contact sufficiently to transfer stress uniformly, so that the beam frequency approaches that of the unbroken state. Thus, crack closure depends to some extent on surface roughness and on elastic properties, but sufficient registry of the faces can be achieved under compression to transfer the load uniformly across the fracture interface and maintain the faces in contact during vibration.

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APPENDIX. EXAMPLE OF FREQUENCY DEPENDENCE ON AXIAL LOAD OF A BEAM CONTAINING CRACKS

This appendix presents a simple example of how the frequency of an axially loaded beam can be modified by changes in stiffness caused by crack closure. We assume a cylindrical beam of material of length L , radius r_1 , and uncracked modulus E , and a set of N regularly spaced annular cracks in the outer surface of the beam (Fig. A.1). The cracks have outer radius r_1 , inner radius r_0 , and maximum crack opening displacement d , where $(Nd) \ll L$. At a certain axial load, P_0 , the cracks close significantly. At the same time, since $(Nd) \ll L$, the overall length change of the sample can be ignored as a first approximation. The sample bulk density ρ is related to the sample mass M and cross-sectional area A , where $A = \pi r_1^2$, and is given by $\rho = M/(AL)$. The change in density under loading and crack closure is also ignored as a first approximation.

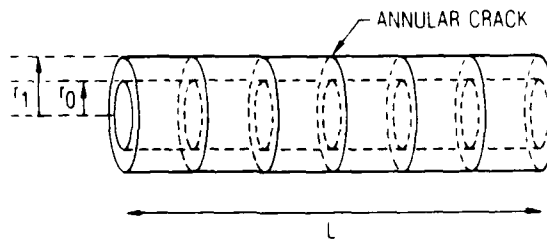


Fig. A.1. Cylindrical Beam with Annular Cracks

A.1 FREQUENCY VERSUS LOAD--CRACKS OPEN

The frequency versus load for the material can now be calculated based on the properties for small vibrations at small loading, $P < P_c$, when the cracks remain open, and assuming that the crack spacing, L/N , is less than the width of the annulus, $r_1 - r_0$. In this case, the beam consists of an undamaged core of radius r_0 and an outer shell of cracked material that carries essentially no tensile or compressive load and serves as dead weight (Ref. 9). From Eqs. (1) and (3)

$$f_0 = \frac{1}{2L} P_b^{1/2} (\rho A)^{-1/2} \quad (A.1)$$

$$f = f_0 (1 - P/P_b)^{1/2} \quad (A.2)$$

$$P < P_c$$

where $P_b = \pi^2 EI/L^2$ and $I = \pi r_0^4/4$.

A.2 FREQUENCY VERSUS LOAD--CRACKS CLOSED

The same relations for the beam when P is greater than P_c and the cracks are effectively closed by the axial load, and remain closed during small vibrations, are calculated from Eqs. (1) and (3) as

$$f'_0 = \frac{1}{2L} P_b'^{1/2} (\rho A)^{-1/2} \quad (A.3)$$

$$f' = f'_0 (1 - P/P_b')^{1/2} \quad (A.4)$$

$$P > P_c$$

where $P_b' = \pi^2 EI'/L^2$ and $I' = \pi r_1^4/4$.

Two f versus P curves are predicted, in Fig. A.2, one for the material with open cracks [from Eq. (A.2)] and one for closed cracks [from Eq. (A.4)]. In a realizable material, crack closure would be expected to be gradual over some load range, rather than abrupt at an exact loading P_c ; therefore, a positive deviation from the f versus P curve would be expected for the cracked material as load is applied, eventually meeting the curve for the closed-crack

material beyond P_c . For this reason, a smooth interpolation between the two curves has been sketched in the range of P near P_c .

The sample in the experiment appears to exhibit this type of bimodular behavior. The frequency of the fractured sample increases with load until it has roughly the same frequency as the unbroken sample, which is analogous to going from the open-crack to the closed-crack state. This model can also serve as a simple example of the effect of crack closure under load on the elastic modulus of a body with many microcracks.

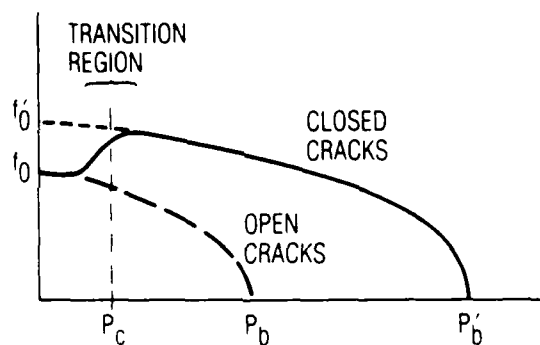


Fig. A.2. Crack Closure under Load and Change of f_0 and P_b

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